THE ELUSIVE HIGGS BOSON(S)

Is it the “God” particle or the “goddamned”* particle?

Jack Gunion
U.C. Davis

*Attributed to Leon Lederman.
Synopsis/Outline

- Precision Electroweak (PEW) data prefer a light Higgs boson.
- Hierarchy prefers a SUSY solution.
- Gauge coupling unification prefers something close to the MSSM.
- Absence of EWSB fine-tuning requires a light SUSY spectrum (in particular, a light $\tilde{t}$) and a light $\tilde{t}$ implies that the SM-like Higgs of SUSY is light.
- Standard MSSM scenarios having a light Higgs with SM-like properties (for PEW perfection) are excluded by LEP.
- Some alternative SUSY models, including the NMSSM (which preserves all good MSSM features and solves the $\mu$ problem) give decay scenarios not ruled out by LEP for lighter Higgs mass.
- LHC strategies for finding the Higgs will need to change.
Reminders about the Higgs mechanism and SM Higgs boson

- The Higgs boson is the quantum fluctuation particle of the Higgs whose vev gives mass to every elementary particle.

- Electroweak symmetry breaking arises from

\[ V = -\mu^2 H^\dagger H + \lambda (H^\dagger H)^2. \]  

Because of the negative quadratic term \( \langle H \rangle = v > 0 \).

- Higgs couplings to SM particles are known.

\[ m_f \propto \lambda_f v, \quad m_W = \frac{gv}{2} \]  

- Higgs cross sections (initiated by SM particles) are determined. Main processes are \( gg \rightarrow h \) and \( qq \rightarrow q'q'WW \) with \( WW \rightarrow h \).
• In the absence of new physics, Higgs decays are also determined by these same couplings.

![Diagram showing branching ratios of Higgs decays versus Higgs mass](image)

**Crucial at low Higgs mass**

• However, Beyond the SM physics could completely alter the Higgs decay patterns.
What will the Higgs(es) look like?

Even though Higgs himself is quite mild mannered, the Higgs boson is not necessarily so, it might more closely resemble Daniel Higgs, i.e. ornery and mischievous:

J. Gunion MPI and MLL Colloquium, April, 2009
What will the Higgs(es) look like?

Even though Higgs himself is quite mild mannered, the Higgs boson is not necessarily so, it might more closely resemble Daniel Higgs, i.e. ornery and mischievous:

J. Gunion MPI and MLL Colloquium, April, 2009
What will the Higgs(es) look like?
What will the Higgs(es) look like?
If you are too impatient to wait to find a Higgs at the LHC, then you can buy one online.

Attraction of the unknown + familiarity breeds contempt = Higgs by far, the most popular particle.
Dear Higgs Boson,

We know you're out there. We can feel you now. We know that you're afraid. You're afraid of us; you're afraid of change. We don't know the future. We didn't write this to tell you how this is going to end. We wrote this to tell you how it's going to begin.

As you know, our Large Hadron Collider has had some setbacks due to a.... uh... "transformer malfunction" but we know it was you. You sabotaged our machine. We hope you've been enjoying your vacation because we're scheduled to restart in September 2009 and we're pissed.

....so run and hide, asshole. Run and hide. If you should get careless and allow yourself to get detected by the Tevatron, we are going to be supremely disappointed; because we want to find you first, and when we do, rest assured we are not going to publish right away. We're going to teach you some manners first.

Love,

CERN

CERN may come to regret this hope.
Do we need a Higgs boson?

- $W_L W_L \rightarrow W_L W_L$, computed perturbatively, violates unitarity without including Higgs boson exchanges.

  In particular, $|\Re a_0| = \frac{s}{32\pi v^2} < \frac{1}{2}$ fails for $s \gtrsim 1$ TeV.

- If the Higgs exchange diagrams of the SM are included, then

  $|\Re a_0| \xrightarrow{s \rightarrow \infty} \frac{m_h^2}{8\pi v^2} < \frac{1}{2}$ for $m_h < 870$ GeV.

What would happen in the former case? Clearly, $W_L W_L$ scattering becomes non-perturbative — to determine the exact manner whereby unitarity is preserved would require some lattice implementation of the $A(W_L W_L)$ calculation using the SM-Higgs Lagrangian.

We do not have the power to do such calculations at the moment. Would $K$-matrix unitarization, the BESS model, .... turn out to be the answer? We simply don’t know.

And, how likely is it that the loop corrections to low-energy LEP, Tevatron, ... observables(which require knowledge of $A(W_L W_L)$ and related) would be consistent with experimental constraints?

The BESS model inputs custodial SU(2) and an effective Higgs mass, $\Lambda$, and high mass resonances to fix things up.
My take: we really need a Higgs boson (or effective equivalent) to make sense of unitarity and precision data simultaneously.

Extra dimensions can provide an alternative (e.g. excited W and Z states that fix up bad high energy behavior), but they have a considerable set of issues, in particular precision data. Although these can be overcome, I will not discuss extra dimension models here.
Quantum Loops: a big source of difficulty for the SM.

Precision Electroweak Data from LEP and Tevatron Creates large tension within the SM because of such loops!

\[ m_W = m_W^0 + c_1 m_t^2 + c_2 \log m_H^2 \]

- LEP PEW overall fit prefers Higgs mass near 80 GeV w. 95% upper bound of about 160 GeV.
- LEP PEW data without hadronic asymmetries prefers Higgs mass of about 50 GeV and below 105 GeV at 95% CL.
- Tevatron W mass + top mass prefers quite light SM Higgs.
- **BUT!** LEP requires SM Higgs heavier than 114 GeV.
  
  And, the Tevatron has excluded a range near \(2m_W\)
The latest plot of $\Delta \chi^2 (\text{PEW})$ vs. $m_H$ is:

At 95$\%$ CL, $m_{\text{min}} < 160$ GeV and the $\Delta \chi^2$ minimum is near 85 GeV when all data are included.

J. Gunion MPI and MLL Colloquium, April, 2009
Figure 1: $\chi^2$ distributions as a function of $m_H$ from the combination of the three leptonic asymmetries $A_{LR}$, $A_{FB}^{\ell}$, $A_{FB}^{\ell}(P_{\tau})$; the three hadronic asymmetries $A_{bFB}$, $A_{cFB}$, $Q_{FB}$ (dashed line); and the three mass-sensitive, nonasymmetric measurements, $m_W$, $\Gamma_Z$, $R_\ell$ (dot-dashed line). The horizontal lines indicate the respective 90% symmetric confidence intervals.

J. Gunion, MPI Colloquium, April 28, 2009

From Chanowitz.
Contours are at one sigma. Red blob =90% CL all data
Electroweak model and constraints on new physics

The parameter $\rho_0$ can be seen as a phenomenological parameter which significantly affects the radiative corrections.
ESCAPE = BSM decays


<table>
<thead>
<tr>
<th>Mode Limit (GeV)</th>
<th>SM modes</th>
<th>$2\tau$ or $2b$ only</th>
<th>$2j$</th>
<th>$WW^* + ZZ^*$</th>
<th>$\gamma\gamma$</th>
<th>$E$</th>
<th>$4e, 4\mu, 4\gamma$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>114.4</td>
<td>115</td>
<td>113</td>
<td>100.7</td>
<td>117</td>
<td>114</td>
<td>114?</td>
</tr>
<tr>
<td>Mode Limit (GeV)</td>
<td>4$b$</td>
<td>4$\tau$</td>
<td>any (e.g. 4$j$)</td>
<td>2$f + E$</td>
<td>90?</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>110</td>
<td>86</td>
<td>82</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Invisible decays don’t “help”
The SM contains the seeds of its own “destruction”.

- the Higgs self coupling should not blow up below scale \( \Lambda \); \( \Rightarrow \) upper bound on \( m_{h^{SM}} \) as function of \( \Lambda \).

- the Higgs potential should not develop a new minimum at large values of the scalar field of order \( \Lambda \); \( \Rightarrow \) lower bound on \( m_{h^{SM}} \) as function of \( \Lambda \).

These two constraints imply that the SM can be valid all the way up to \( M_P \) if \( 130 \lesssim m_{h^{SM}} \lesssim 180 \) GeV.

![Diagram showing constraints on \( m_{h^{SM}} \) vs. \( \Lambda \).](image)

**Figure 1:** Triviality and global minimum constraints on \( m_{h^{SM}} \) vs. \( \Lambda \).
One generic way of having a low LEP limit on $m_H$ is to suppress the $H \to b\bar{b}$ branching ratio by having a light $a$ (or $h$) with $B(H \to a a) > 0.7$ and $m_a < 2m_b$ (to avoid LEP $Z + 4b$ limit at 110 GeV, i.e. above ideal). For $2m_\tau < m_a < 2m_b$, $a \to \tau^+\tau^-$. For $m_a < 2m_\tau$, $a \to jj$.


Since the $Hb\bar{b}$ coupling is so small, very modest $Haa$ coupling suffices.

**An attractive possibility:** $m_H \sim 100$ GeV and $BR(H \to b\bar{b}) \sim 0.1$

Explains largest LEP excess (2.3 sigma).
The 2nd major implication of Quantum Loops: the Hierarchy Problem

The Higgs mass itself acquires a large loop correction from the top quark loop.

\[ m_H^2 = (m_H^0)^2 - c\Lambda^2 \]

We need a light Higgs for unitarity and for PEW, but if the cutoff is large this requires extreme cancellation between the loop and tree-level terms.

Supersymmetry is the only theory that provides a solution and that could potentially be consistent (no high-scale completion required) all the way to the GUT scale. It provides a spin-0 stop whose loop cancels the problem. (fermi-statistics)

\[ \delta m_H^2 \sim c(\Lambda^2 + m_t^2) \]

So long as \( m_t^- \) is not above 1 TeV, cancellation of the quadratics is not too highly tuned.
In the minimal supersymmetric model (MSSM) there is a partner for every SM particle and two Higgs doublet fields $H_u, H_d$.

- The MSSM comes close to being very nice.

If we assume that all sparticles reside at the $\mathcal{O}(1 \text{ TeV})$ scale and that $\mu$ is also $\mathcal{O}(1 \text{ TeV})$, then, the MSSM has two particularly wonderful properties.

1. **Gauge Coupling Unification**

**Standard Model**

<table>
<thead>
<tr>
<th>$\alpha^{-1}$</th>
<th>$\alpha_1^{-1}$</th>
<th>$\alpha_2^{-1}$</th>
<th>$\alpha_3^{-1}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Q$ (GeV)</td>
<td>$10^4$</td>
<td>$10^8$</td>
<td>$10^{12}$</td>
</tr>
</tbody>
</table>

**MSSM**

<table>
<thead>
<tr>
<th>$\alpha^{-1}$</th>
<th>$\alpha_1^{-1}$</th>
<th>$\alpha_2^{-1}$</th>
<th>$\alpha_3^{-1}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Q$ (GeV)</td>
<td>$10^4$</td>
<td>$10^8$</td>
<td>$10^{12}$</td>
</tr>
</tbody>
</table>

**Figure 4:** Unification of couplings constants ($\alpha_i = g_i^2/(4\pi)$) in the minimal supersymmetric model (MSSM) as compared to failure without supersymmetry.
2. **RGE EWSB**

**Figure 5:** Evolution of the (soft) SUSY-breaking masses or masses-squared, showing how $m_{H_u}^2$ is driven $< 0$ at low $Q \sim \mathcal{O}(m_Z)$.

Recall that a negative tree-level mass is needed to have symmetry breaking in the vacuum leading to $<H> = \text{non-zero}$. In SUSY, this is almost automatic.

NB: the scale evolution depicted in the above plots is also due to the fact that constants are not constants in QFT --- they depend on the scale of measurement due to loop corrections.
In fact, the MSSM not only solves the hierarchy problem, but also predicts that $m_h < 110$ GeV when $m_{\tilde{t}} < 400$ GeV.

MSSM Higgs sector: $h, H, A$ with $h$ typically SM-like unless it is very light and $H$ is SM-like.

Such a light $h$ would be perfect for PEW constraints (not to mention baryogenesis), but also such a light stop solves the “electroweak” fine-tuning problem.

The degree of electroweak fine-tuning, $F$, specifies how precisely the GUT scale parameters must be tuned in order to get the observed value of the $Z$ mass. $F < 10$ (no worse than 10% tuning) is desirable and is obtained if $m_{\tilde{t}} < 400$ GeV.

The problem: the light Higgs of the MSSM decays like the SM Higgs and is basically excluded for $m_h < 114$ GeV. This implies that $m_{\tilde{t}} > 800$ GeV which in turn implies $F > 50 = \text{very bad!}$

What is needed is a SUSY model for which the stop mass can be low but for which the resulting light <100 GeV Higgs is not excluded by LEP.

LEP exclusion can be avoided by having unusual decays as seen earlier.
My favorite SUSY model is the Next to Minimal Supersymmetric Model (NMSSM). It has an \( a \) of the type needed and retains the supersymmetric solution to the hierarchy problem.

The \( a \) comes mainly from the singlet, \( S \), field that solves the famous mu-problem of the MSSM and was the initial motivation for the NMSSM.

\[
W \ni \mu \hat{H}_u \hat{H}_d \quad \text{MSSM} \quad \text{vs.} \quad W \ni \lambda \hat{S} \hat{H}_u \hat{H}_d \rightarrow \lambda \langle S \rangle \hat{H}_u \hat{H}_d \quad \text{NMSSM}
\]

\( A_\lambda, A_\kappa \) are the new soft-SUSY-breaking parameters.

The required properties of the \( a \) are natural in the NMSSM. In particular, there is a \( U(1)_R \) symmetry in the limit of \( A_\lambda, A_\kappa \rightarrow 0 \) that, if exact, predicts that the \( a \) would be massless. This symmetry, if exact at the GUT scale, is weakly broken in evolving down from the GUT scale.

And, very importantly, the NMSSM yields (like the MSSM) gauge coupling unification and “radiative” electroweak symmetry breaking.
Other SUSY decays that would escape strongest LEP limits:

\[ h \to \tilde{\chi}_1^0 + \tilde{\chi}_2^0 \to \tilde{\chi}_1^0 + \tilde{\chi}_1^0 + f\bar{f} \to E_{miss} + f\bar{f} \]
\[ h \to \tilde{\chi}_1^0 + \tilde{\chi}_1^0 \to \tilde{G} + \tilde{G} + \gamma + \gamma \to E_{miss} + \gamma + \gamma \]

LEP limits for the latter are not known, but maybe they would have noticed this decay if the Higgs were below 114 GeV?

Note: the above are some natural cases assuming R-parity conserving SUSY so that there will be a dark matter candidate. There are many more SUSY models with unusual Higgs decays related to R-parity violation and similar that would, however, not allow for a dark matter particle.

There are also many BSM approaches in which the electroweak Higgs (i.e. the one with ZZ coupling) decays invisibly.

As noted earlier, LEP constrains an invisibly decaying Higgs as strongly as if it decayed a la SM. From the PEW perspective this is not desirable.
Detecting the light $h$ of the NMSSM

LHC

All standard LHC channels fail: e.g. $B(h \rightarrow \gamma\gamma)$ is much too small because of large $B(h \rightarrow aa)$.

The possible new LHC channels include:

1. $gg \rightarrow h \rightarrow aa \rightarrow 4\tau$ and $2\tau + \mu^{+}\mu^{-}$

Always use $\mu$ tag for accepted events. $2\tau + 2\mu$ is main signal source after cuts.

There is an actual D0 analysis (A. Haas et. al.) of this mode using about $L \sim 4 \text{ fb}^{-1}$ of data. There is even a small $\sim 1\sigma$ excess. They estimate about $L \sim 40 \text{ fb}^{-1}$ would be needed for a $5\sigma$ signal but even a $\sim 3\sigma$ signal
as possible for $L \sim 20 \text{ fb}^{-1}$ would be exciting.

Presented at the Moriond winter conference.
A theoretical study (Wacker et al.) suggests that a $> 3\sigma$ signal would be possible at the LHC after the first 3 years or so of running.

2. $WW \rightarrow h \rightarrow aa \rightarrow \tau^+\tau^- + \tau^+\tau^-$.  

Key will be to tag relevant events using spectator quarks and require very little activity in the central region by keeping only events with 4 or 6 tracks.

Looks moderately promising but far from definitive results at this time (see, A. Belyaev et al., arXiv:0805.3505 [hep-ph] and our work, JFG+Tait+Z. Han, below).

More shortly.

3. $t\bar{t}h \rightarrow t\bar{t}aa \rightarrow t\bar{t} + \tau^+\tau^- + \tau^+\tau^-$.  

Study begun.

4. $\tilde{\chi}_2^0 \rightarrow h\tilde{\chi}_1^0$ with $h \rightarrow aa \rightarrow 4\tau$.

(Recall that the $\tilde{\chi}_2^0 \rightarrow h\tilde{\chi}_1^0$ channel provides a signal in the MSSM when $h \rightarrow b\bar{b}$ decays are dominant.)
5. Last, but definitely not least: diffractive production $pp \rightarrow pph \rightarrow ppX$.

The mass $M_X$ can be reconstructed with roughly a $1 - 2$ GeV resolution, potentially revealing a Higgs peak, independent of the decay of the Higgs.

The event is quiet so that the tracks from the $\tau$’s appear in a relatively clean environment, allowing track counting and associated cuts.

Our (JFG, Forshaw, Pilkington, Hodgkinson, Papaefstathiou: arXiv:0712.3510) results are that one expects about 3 clean, i.e. reconstructed and tagged, events with very small background ($\sim 0.1$ event) per $90$ fb$^{-1}$ of luminosity.

$\Rightarrow$ clearly a high luminosity game.

We estimate the significance, $S$, of the observation by equating the probability of $s + b$ events given a Poisson distribution with mean $b$ to the probability of $S$ standard deviations in a Gaussian distribution.

Signal significances are plotted in Fig. 6 for a variety of luminosity and
triggering assumptions.

Figure 6: (a) The significance for three years of data acquisition at each luminosity. (b) Same as (a) but with twice the data. Different lines represent different $\mu$ trigger thresholds and different forward detector timing. Some experimentalists say more efficient triggering is possible, doubling the number of events at given luminosity.

CMS folk claim we can increase our rates by about a factor of 2 to 3 using additional triggering techniques.
The Collinearity Trick

- Since $m_a \ll m_h$, the $a$'s in $h \rightarrow aa$ are highly boosted.
  $\Rightarrow$ the $a$ decay products will travel along the direction of the originating $a$.
  $\Rightarrow p_a \propto \sum \text{visible 4-momentum} \text{ of the charged tracks in its decay.}$
  Labeling the two $a$'s with indices 1 and 2 we have
  \[ p_i^{vis} = f_i p_{a,i} \] (25)
  where $1 - f_i$ is the fraction of the $a$ momentum carried away by neutrals.

- $pp \rightarrow pph$ case
  The accuracy of this has now been tested in the $pp \rightarrow pph$ case, and gives an error for $m_h$ of order 5 GeV, but this is less accurate than $m_h$ determination from the tagged protons and so is not used.
However, we are able to make four $m_\alpha$ determinations per event.

**Figure 7:** (a) A typical $\alpha$ mass measurement. (b) The same content as (a) but with the breakdown showing the 4 Higgs mass measurements for each of the 6 events, labeled 1 – 6 in the histogram.

Figure 7 shows the distribution of masses obtained for 180 fb$^{-1}$ of data collected at $3 \times 10^{33}$ cm$^{-2}$s$^{-1}$, corresponding to about 6 Higgs events and therefore 24 $m_\alpha$ entries. In the right-hand figure the integer in each box labels one of the 6 signal events.
By considering many pseudo-data sets, we conclude that a typical experiment would yield $m_a = 9.3 \pm 2.3$ GeV, which is in re-assuringly good agreement with the input value of 9.7 GeV.

- **$WW \rightarrow h$**

For $m_h = 100$ GeV and SM-like $WWh$ coupling, $\sigma(WW \rightarrow h) \sim 7$ pb, implying $7 \times 10^5$ events before cuts for $L = 100$ fb$^{-1}$.

In this case, we do not know the longitudinal momentum of the $h$, but we should have a good measurement of its transverse momentum from the tagging jets and other recoil jets.

In fact, in this case, $p_T^h$ must be large enough that the $a$'s are not back to back; this is the case for almost all events even before cuts.

We then have the two equations that can be solved for $f_1$ and $f_2$:

$$p_h^x = \frac{(p_{1 \, \text{vis}}^x)}{f_1} + \frac{(p_{2 \, \text{vis}}^x)}{f_2} \quad p_h^y = \frac{(p_{1 \, \text{vis}}^y)}{f_1} + \frac{(p_{2 \, \text{vis}}^y)}{f_2}. \quad (26)$$

Of course, this follows very much the same pattern as in $WW \rightarrow h_{\text{SM}}$ with $h_{\text{SM}} \rightarrow \tau^+\tau^-$ decays. Use of the collinear $\tau$ decay approximation
and using the same equations for the visible $\tau$ decay products yields a pretty good $h_{\text{SM}}$ mass peak in the LHC studies done of this mode.

- A signal only Monte-Carlo run without lepton or tag jet momentum smearing yields encouraging results

Figure 8: (a) A typical $h$ mass distribution. (b) A typical $\alpha$ mass distribution. No cuts imposed; signal only

- We have now developed cuts that we are relatively certain will control backgrounds nicely. These cuts do not change the mass reconstruction above significantly, even after including PGS (CMS) smearing.
The ILC

At the ILC, there is no problem since $e^+e^- \rightarrow ZX$ will reveal a $M_X \sim m_h \sim 90 - 100$ GeV peak no matter how the $h$ decays.

If there are many Higgs, then the excesses in various bins of $M_X$ will be apparent even if there is a broad sort of spectrum and $X$ has a mixture of decays.

But the ILC is decades away.

Note: collinearity trick also works well for $h \rightarrow aa \rightarrow \tilde{G}\gamma + \tilde{G}\gamma$ if you have some transverse momentum for the Higgs.
A few further points regarding a light $a$

- The $a$ is largely singlet: $a = \cos \theta_A a_{MSSM} + \sin \theta_A a_S$ with $\cos \theta_A$ small.

- Define a generic coupling to fermions by
  \[
  \mathcal{L}_{af\bar{f}} \equiv iC_{af\bar{f}} \frac{ig_2 m_f}{2m_W} \bar{f} \gamma_5 f a, \quad \text{then} \quad C_{ab\bar{b}} = \cos \theta_A \tan \beta \quad (13)
  \]

- The extracted $C_{ab\bar{b}}$ limits (JFG, arXiv:0808.2509; see also Ellwanger and Domingo) are quite model-independent. The extracted limits on $C_{ab\bar{b}}$ appear in Fig. 5.

- The most unconstrained region is that with $m_a > 8 \text{ GeV}$, especially $9 \text{ GeV} < m_a < 12 \text{ GeV}$. = region with least "light-$a_1$" tuning in NMSSM.

- Except for this region, a further factor of 3 improvement to $C_{ab\bar{b}} < 0.3$ would start to rule out or observe the $a = a_1$ of the most favored NMSSM scenarios.
In the $\sim 9 \text{ GeV} \lesssim m_a \lesssim 12 \text{ GeV}$ region only the OPAL limits are relevant.

Those presented depend upon how the $a \leftrightarrow \eta_b$ states mixing is modeled. A particular model (Drees+Hikasa: Phys.Rev.D41:1547,1990) is employed.

**Actually, the Tevatron has a chance to make a valuable contribution with large integrated L.**
Figure 5: 90% CL limits on \( \frac{\sigma(a)B(a\rightarrow\mu^+\mu^-)}{\sigma(\Upsilon)B(\Upsilon\rightarrow\mu^+\mu^-)} \) at small \(|y|\) for \( L = 630 \) pb\(^{-1}\), compared to expectations for the \( a \) for \( C_{ab\bar{b}} = \tan \beta = 1/C_{att} = 1, 2, 3 \) in the 2HDM-II. Also shown (□'s) are the predictions for the NMSSM with \( \tan \beta = 10 \) and \( \cos \theta_A = 0.1 \) for which \( C_{ab\bar{b}} = \tan \beta \cos \theta_A = 1 \) and \( C_{att} = \cot \beta \cos \theta_A = 1/100 \) — not much different from the \( C_{ab\bar{b}} = \tan \beta = 1/C_{att} = 1 \) case.
Translating the 630 pb$^{-1}$ results into limits on $C_{abb}$ gives the dotted histogram in the 6 – 9 GeV region in Fig. 6 (below):

Figure 6: Limits on $C_{abb}$ including those from the Tevatron analysis.

The Tevatron limits are the best for $\sim 8$ GeV $< m_a < \sim 9$ GeV.
• If you really want to go to extremes, imagine many Higgs bosons in the mass region below 100 GeV. If in SUSY context, use multiple singlets mixing with the two doublets to avoid losing gauge coupling unification.
• Each would decay in some exotic, LEP-escaping manner and each would have weaker coupling to ZZ than the SM Higgs and thus lower rate anyway.
• Such scenarios arise in deconstructed unHiggs theories.
• It is easy to get an effectively very low average Higgs mass in the precision electroweak sense.
• Sharing of the top loop among many doublet Higgs bosons delays the quadratic hierarchy problem to higher scales. But, not good for coupling unification --- in SUSY context, keep SUSY scale near 1 TeV.
• Detection of such a continuum of Higgs at the LHC would be really hard!
Meanwhile, all I can do is watch and wait (but maybe not from such a close distance).
Conclusions: where is Higgs?

I am going crazy waiting for the Higgs and it is premature to claim we know where or how to find it.

We could have simply missed it at LEP.

There is a strong preference for a rather light Higgs boson --- PEW, SUSY+EWSB fine-tuning, ....

It must decay in non-SM ways to avoid LEP limits.

Many very attractive models based on SUSY allow for the needed kinds of decays.

Searches for a Higgs decaying in exotic ways are quite challenging at hadron colliders.

If no Higgs is seen after a number of LHC years, is it safe to conclude that there is no Higgs?

Check WW scattering (hard!).

Build ILC/CLIC (2020, but Higgs detection easy once built).

If the light Higgs/SUSY scenario is correct, SUSY particles should be light (as preferred by no EWSB fine tuning) and easily seen at the LHC!